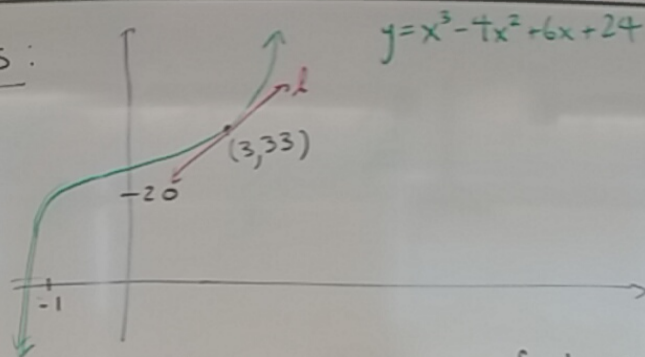


Given any curve, the instantaneous rate of change at a point  $(a, f(a))$  is given by computing the derivative at that point.

$$f'(a)$$

It turns out this is the slope of the tangent line,  $l$ , in the picture above.

Examples:



The instantaneous rate of change at  $(3, 33)$  is given by  $f'(3)$ .

$$\text{And } f'(x) = 3x^2 - 8x + 6$$

$$\text{So } f'(3) = 3(3)^2 - 8(3) + 6$$

$$= 9$$

So, the slope of line  $l$  is  $\boxed{9}$ .

What

$$f(x) = 3x^{12} + 4x^3$$

$$f'(x) = 36x^{11} + 12x^2$$

$$f''(x) = 396x^{10} + 24x$$

$$f^{(3)}(x) = 3960x^9$$